# Attention, exhaustivity and non-cooperativity 

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## Two puzzles

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## Part I

1. Diagnosis
2. Theory
3. Results
4. Discussion

## 1. Diagnosis

1.1. The problem
1.2. Existing approaches
1.3. Towards a solution

### 1.1. The problem

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Wrong, it does!

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(5) I'm asking the wrong person, but who came to the party? John and Bill came. $\leadsto$ Not Mary.


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## 2. Theory

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2.2. Semantics
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(3) a. John came, or Mary, or John and Mary.

$$
\begin{array}{r}
p \vee q \vee(p \wedge q) \\
p \\
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\end{array}
$$

b. John came.
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$A$ entails $B, A \vDash B$, iff
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Now, (3c) $\vDash(3 a)$, but (3b) $\neq(3 a)$.

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The relevant maxims

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It was raining.

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It was raining. $\leadsto$ If it rained, John $\{$ went / didn't go $\}$.


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## 3. Results

3.1. Examples
3.2. Formal results
3.3. And more conceptually...

### 3.1. Examples

(3) a. John came, Mary came, or both came $(p \vee q \vee(p \wedge q))$ b. John came. (p)
c. John came, or Mary and John. $(p \vee(p \wedge q))$

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(Quality)
2. $s \nsubseteq|q|$
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p \vee(p \wedge q) \vDash p \vee q \vee(p \wedge q)
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(Quantity)

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(3) a. John came, Mary came, or both came $(p \vee q \vee(p \wedge q))$
b. John came. (p)

1. $s \subseteq|p|$
2. $s \nsubseteq|q|$
(Quality)
(Quantity)
c. John came, or Mary and John. $(p \vee(p \wedge q))$
3. $s \subseteq|p \vee(p \wedge q)|=|p|$
(Quality)
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5.     - 

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### 3.2. Formal results

Recall: $A$ entails $Q, A \vDash Q$, iff
(i) $\cup A \subseteq \cup Q$; and
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Main conclusion:

- If pragmatic reasoning is sensitive to attentive content (which it must be, to distinguish between (3b) and (3c));
- then exhaustivity is a conversational implicature.


## 4. Discussion

4.1. 'Alternatives'
4.2. Semantics
4.3. Semantic desiderata
4.4. 'Gricean'?
4.5. Grice vs. grammar
4.6. Other maxims of Relation
4.7. Relatedness and knowledge
4.8. Logical relatedness

## 4.1. 'Alternatives'

Existing approaches (since forever):

- 'Why did the speaker not say " $p \wedge q$ " ?'


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- Ignorance is no excuse.
- Hence something stronger is implied: exhaustivity.


## Beware:

- These 'alternatives' are fully determined by the maxims.
- Speakers need not reason in terms of alternatives.


### 4.2. Semantics

Restriction
$A$ restricted to $b, A_{b}:=\{a \cap b \mid a \in A, a \cap b \neq \varnothing\}$
Semantics (Roelofsen, 2011)

$$
\begin{aligned}
& \text { 1. }[p]=\{\{w \in \text { Worlds } \mid w(p)=\text { true }\}\} \\
& \text { 2. }[\neg \varphi]=\{\overline{\cup[\varphi]\}} \text { if } \overline{\cup[\varphi]} \text { is nonempty; } \varnothing \text { otherwise. } \\
& \text { 3. }[\varphi \vee \psi]=([\varphi] \cup[\psi])_{|\varphi| \cup|\psi|}=[\varphi] \cup[\psi] \\
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Attentive semantics is not the only suitable semantics:

- Unrestricted Inquisitive Sem. (Ciardelli, 2009; Westera, 2012)


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Attentive semantics is not the only suitable semantics:

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Minimally, the semantics must lack the absorption laws:

- Absorption: $p \vee(p \wedge q) \equiv p \equiv p \wedge(p \vee q)$


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- Questions, the responses to which may be exhaustified, are not partitions.
(cf. Groenendijk and Stokhof, 1984; cf. 'mention-some').
- Wh-words are existential quantifiers over sets.


## 4.4. 'Gricean'?

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- The semantics treats informative content classically.


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Besides: this is the only way.

### 4.5. Grice vs. grammar

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Main arguments (Chierchia, et al., 2008):

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Response:

- Grice can do it; and the grammatical approach needs him.


### 4.6. Other maxims of Relation

i. $R_{s} \vDash Q$
(mine)

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& \text { i. } R_{s} \vDash Q \\
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(Roberts's (1996) contextual entailment)

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ii. and iii. are too strong:

- The participants need not already know how $R$ is relevant.
- They need only be able to figure it out. (left implicit here)
(4) Did John go to the party? It was raining. $\leadsto$ If it rained, John $\{$ went / didn't go $\}$.


### 4.7. Relatedness and knowledge

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Within a world, everything is related.

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Just as [logical consequence] rules the validity of argumentation, [logical relatedness] rules the coherence of information exchange.
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Logical consequence is logical relatedness.

End of Part I

## Two puzzles

(1) Of John, Bill and Mary, who came to the party?
a. John came $\downarrow$. $\sim$ Mary and Bill didn't.
b. John came $\nearrow$.
$\leadsto$...wait, there's more.
$\leadsto \ldots$ perhaps that implies sth. about M\&B?
$\leadsto$...but I'm not sure.
$\leadsto$...did I make myself clear?

## Part II

5. Analysis
6. Results
7. Discussion
8. Analysis

## 5. Analysis

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(1) Of John, Bill and Mary, who came to the party?
b. John came $\lambda^{L}$.
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1. The final rise marks the violation of a maxim.

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2. Its pitch conveys the severity of the violation:
${ }_{\lambda}{ }^{H}$ : Quality/Manner;
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(cf. Ward \& Hirschberg, 1992;
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This proposal is new in its generality, not in spirit.

## 6. Results

6.1. Example
6.2. Formal results
6.3. General results

### 6.1. Example

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(8) Of J and M , who came to the party?
$(p \vee q \vee(p \wedge q))$
(p)

1. $s \subseteq|p|$
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(Quality)
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Furthermore:

- Exhaustivity disappears in all readings except Manner.


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4. The speaker doesn't think she's clear, concise, etc.

## Readings

$\checkmark$...wait, there's more.
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Furthermore:

- Exhaustivity disappears in all readings except Manner.
- Complete answers lack Relation/Quantity reading.


### 6.1. Example

(8) Of J and M , who came to the party? John came $\nearrow$.

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Relation violation on singleton answer And if responding $\{a\}$ to $Q$ for some $a \in Q$ : for some $q \in Q, s \nsubseteq \bar{a} \cup \bar{q}$ and $s \nsubseteq \bar{a} \cup q$

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Quantity violation
For some $Q^{\prime} \subseteq Q, s \subseteq \cup Q^{\prime}$ and $\cup R \nsubseteq \cup Q^{\prime}$.

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The enabling innovation is the 'attentive' maxim of Relation.

## 7. Discussion

7.1. Evoked questions
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7.3. Objective/subjective cooperativity

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Connecting this to the literature is a work in progress.
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Future work!

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But an account based on objective maxims would also work:

- Final rise: 'For some maxim, I'm not sure whether or how I comply with it'.

End of Part II

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## Part II:

- If, furthermore, the final rise conveys the violation of a maxim
- then the many readings of the final rise are predicted.


## The End

## Articles

- Exhaustivity through the maxim of Relation (LENLS proceedings, see staff.science.uva.nl/~westera/)
- 'Attention, I'm violating a maxim!' (submitted, available through me)

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## Appendix. 'Embedded' implicatures

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The 'embedded' implicature of (6) is in fact predicted.

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